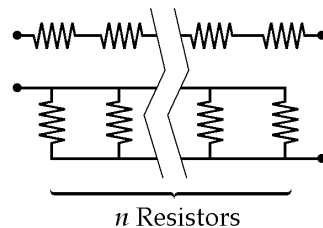


57. A voltage ΔV is applied to a series configuration of n resistors, each of value R . The circuit components are reconnected in a parallel configuration, and voltage ΔV is again applied. Show that the power consumed by the series configuration is $1/n^2$ times the power consumed by the parallel configuration.



Solution

When connected in series, the equivalent resistance is

$$R_{eq} = R_1 + R_2 + \dots + R_n = nR$$

Thus, the power consumed by the series configuration is

$$\mathcal{P}_s = (\Delta V)I = (\Delta V) \left(\frac{\Delta V}{R_{eq}} \right) = \frac{(\Delta V)^2}{R_{eq}} = \frac{(\Delta V)^2}{nR}$$

For the parallel connection, the power consumed by each individual resistor is

$$\mathcal{P}_1 = \frac{(\Delta V)^2}{R}$$

and the total power consumption by the parallel configuration is

$$\mathcal{P}_p = n\mathcal{P}_1 = \frac{n(\Delta V)^2}{R}$$

Therefore,

$$\frac{\mathcal{P}_s}{\mathcal{P}_p} = \left(\frac{(\Delta V)^2}{nR} \right) \left(\frac{R}{n(\Delta V)^2} \right) = \frac{1}{n^2}$$

or

$$\mathcal{P}_s = \frac{1}{n^2} \mathcal{P}_p$$

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